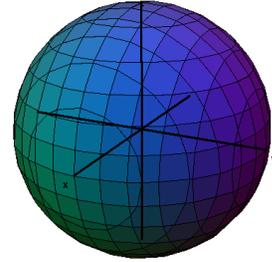


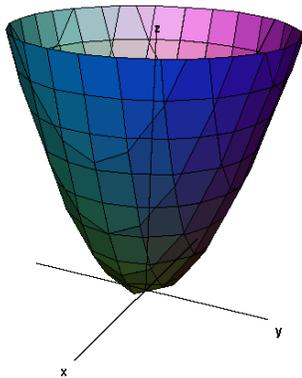
Ellipsoid: $\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$

- All traces are ellipses.
- If $a = b = c$, the ellipsoid is a sphere.



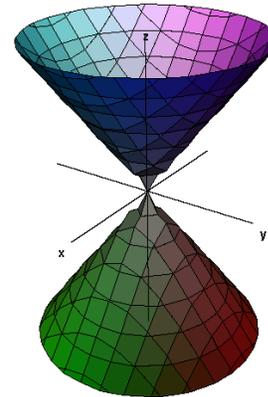
Sphere: $x^2 + y^2 + z^2 = r^2$

- All Traces are circles.



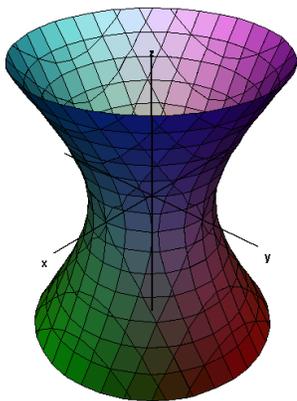
Elliptic Paraboloid: $\frac{z}{c} = \frac{x^2}{a^2} + \frac{y^2}{b^2}$

- Horizontal traces are ellipses.
- Vertical traces are parabolas.
- The variable raised to the first power indicates the axis of the paraboloid.



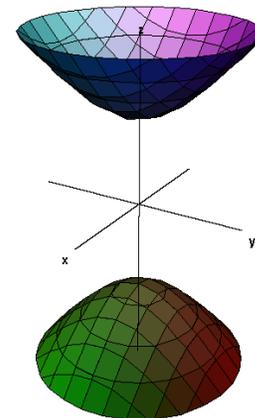
Cone: $\frac{z^2}{c^2} = \frac{x^2}{a^2} + \frac{y^2}{b^2}$

- Horizontal traces are ellipses.
- Vertical traces in the planes $x = k$ and $y = k$ are hyperbolas if $k \neq 0$ but are pairs of lines if $k = 0$



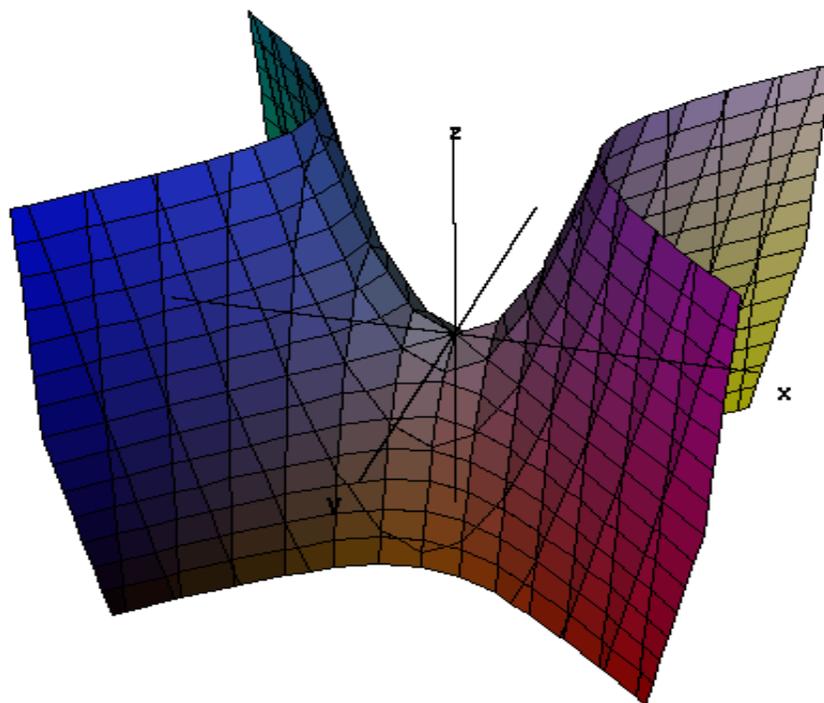
Hyperboloid of One Sheet: $\frac{x^2}{a^2} + \frac{y^2}{b^2} - \frac{z^2}{c^2} = 1$

- Horizontal traces are ellipses.
- Vertical traces are hyperbolas.
- The axis of symmetry corresponds to the variable whose coefficient is negative.



Hyperboloid of Two Sheets: $-\frac{x^2}{a^2} - \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$

- Horizontal traces in $z = k$ are ellipses if $k > c$ or $k < -c$.
- Vertical traces are hyperbolas.
- The two minus signs indicates two sheets.



Hyperbolic Paraboloid:
$$\frac{z}{c} = \frac{x^2}{a^2} - \frac{y^2}{b^2}$$

- Horizontal traces are hyperbolas.
- Vertical traces are parabolas.
- The case where $c > 0$ is illustrated.